

Deep Reinforcement Learning, VAE

Milan Straka

■ May 6, 2024

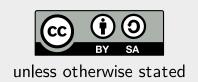








Charles University in Prague Faculty of Mathematics and Physics Institute of Formal and Applied Linguistics



Reinforcement Learning



Reinforcement Learning

Reinforcement Learning



Reinforcement learning is a machine learning paradigm, different from *supervised* and *unsupervised learning*.

The essence of reinforcement learning is to learn from *interactions* with the environment to maximize a numeric *reward* signal. The learner is not told which actions to take, and the actions may affect not just the immediate reward, but also all following rewards.



RL

NAS

History of Reinforcement Learning



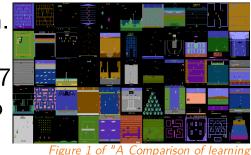
Develop goal-seeking agent trained using reward signal.

- Optimal control in 1950s Richard Bellman
- Trial and error learning since 1850s
 - Law and effect Edward Thorndike, 1911
 - Responses that produce a satisfying effect in a particular situation become more likely to occur again in that situation, and responses that produce a discomforting effect become less likely to occur again in that situation
 - Shannon, Minsky, Clark&Farley, ... 1950s and 1960s
 - Tsetlin, Holland, Klopf 1970s
 - Sutton, Barto since 1980s

Reinforcement Learning Successes



- Human-level video game playing (DQN) 2013 (2015 Nature), Mnih. et al, Deepmind.
 - After 7 years of development, the Agent57 beats humans on all 57 Atari 2600 games, achieving a mean score of 4766% compared to human players.
- AlphaGo beat 9-dan professional player Lee Sedol in Go in Mar 2016.
 - After two years of development, AlphaZero achieved best performance in Go, chess, shogi, being trained using self-play only.



algorithms on the Arcade Learning https://arxiv.org/abs/1410.8620



Figure 2 of "A general reinforcement learning algorithm that masters chess, shogi, and Go through self-play" by David Silver et al.

Impressive performance in Dota2, Capture the flag FPS, StarCraft II, ...

Reinforcement Learning Successes



- Neural Architecture Search since 2017
 - automatically designing CNN image recognition networks surpassing state-of-the-art performance
 - NasNet, EfficientNet, EfficientNetV2, ...
 - AutoML: automatically discovering
 - architectures (CNN, RNN, overall topology)
 - activation functions
 - optimizers
 - **.**..
- Controlling cooling in Google datacenters directly by AI (2018)
 - reaching 30% cost reduction
- Optimize nondifferentiable loss
 - improved translation quality in 2016
 - Reinforcement learning from human feedback (RLHF) is used during chatbot training (ChatGPT, ...)
- Discovering discrete latent structures

MDP

Multi-armed Bandits





It's a Jungle out there! by HAGEN HAGEN @ 2001 Compulsive gambling Hagen Cartoons: http://www.hagencartoons.com

http://www.infoslotmachine.com/img/one-armed-bandit.jpg

https://hagencartoons.com/cartoon170.gif

RL

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Multi-armed Bandits



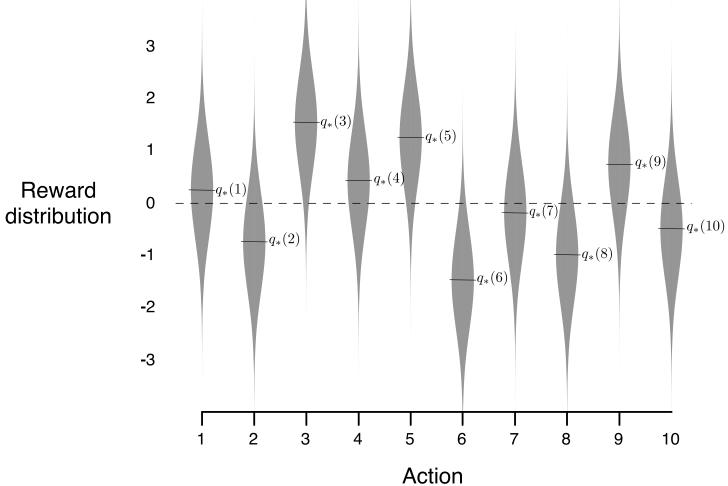


Figure 2.1 of "Reinforcement Learning: An Introduction", http://www.incompleteideas.net/book/the-book-2nd.html

Multi-armed Bandits



We start by selecting action A_1 , which is the index of the arm to use, and we get a reward of R_1 . We then repeat the process by selecting actions A_2 , A_3 , ...

Let $q_*(a)$ be the real **value** of an action a:

$$q_*(a) = \mathbb{E}[R_t|A_t = a].$$

Denoting $Q_t(a)$ our estimated value of action a at time t (before taking trial t), we would like $Q_t(a)$ to converge to $q_*(a)$. A natural way to estimate $Q_t(a)$ is

$$Q_t(a) \stackrel{\text{def}}{=} rac{ ext{sum of rewards when action } a ext{ is taken}}{ ext{number of times action } a ext{ was taken}}.$$

Following the definition of $Q_t(a)$, we could choose a **greedy** action A_t as

$$A_t \stackrel{ ext{ iny def}}{=} rg \max_a Q_t(a).$$

ε -greedy Method



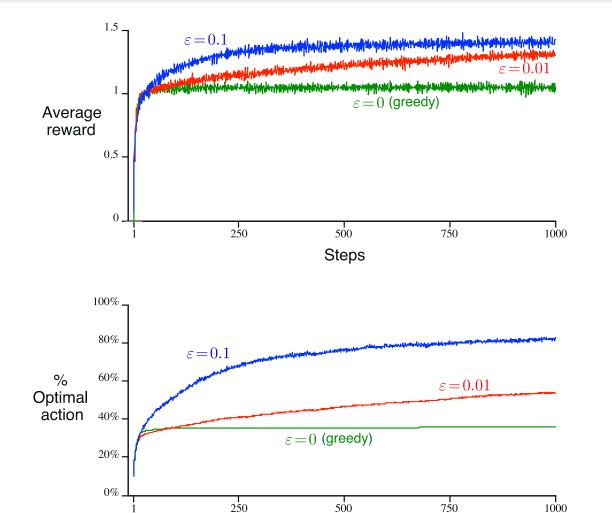
Exploitation versus Exploration

Choosing a greedy action is **exploitation** of current estimates. We however also need to **explore** the space of actions to improve our estimates.

An ε -greedy method follows the greedy action with probability $1-\varepsilon$, and chooses a uniformly random action with probability ε .

ε -greedy Method

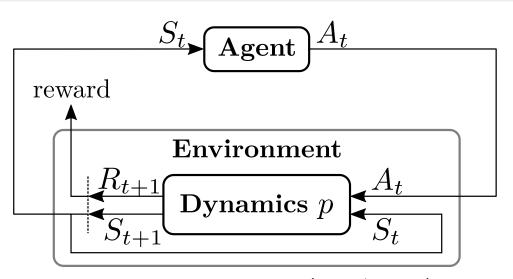




Steps
Figure 2.2 of "Reinforcement Learning: An Introduction", http://www.incompleteideas.net/book/the-book-2nd.html

Markov Decision Process





A Markov decision process (MDP) is a quadruple (S, A, p, γ) , where:

- S is a set of states.
- \mathcal{A} is a set of actions,
- $ullet p(S_{t+1}=s',R_{t+1}=r|S_t=s,A_t=a)$ is a probability that action $a\in\mathcal{A}$ will lead from state $s \in \mathcal{S}$ to $s' \in \mathcal{S}$, producing a **reward** $r \in \mathbb{R}$,
- ullet $\gamma \in [0,1]$ is a **discount factor** (we always use $\gamma = 1$ and finite episodes in this course).

Let a **return** G_t be $G_t \stackrel{\text{def}}{=} \sum_{k=0}^{\infty} \gamma^k R_{t+1+k}$. The goal is to optimize $\mathbb{E}[G_0]$.

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Episodic and Continuing Tasks



If the agent-environment interaction naturally breaks into independent subsequences, usually called **episodes**, we talk about **episodic tasks**. Each episode then ends in a special **terminal state**, followed by a reset to a starting state (either always the same, or sampled from a distribution of starting states).

In episodic tasks, it is often the case that every episode ends in at most H steps. These **finite-horizon tasks** then can use discount factor $\gamma=1$, because the return $G\stackrel{\text{def}}{=} \sum_{t=0}^H \gamma^t R_{t+1}$ is well defined.

If the agent-environment interaction goes on and on without a limit, we instead talk about **continuing tasks**. In this case, the discount factor γ needs to be sharply smaller than 1.

Policy



A **policy** π computes a distribution of actions in a given state, i.e., $\pi(a|s)$ corresponds to a probability of performing an action a in state s.

We will model a policy using a neural network with parameters $oldsymbol{ heta}$:

$$\pi(a|s;\boldsymbol{\theta}).$$

If the number of actions is finite, we consider the policy to be a categorical distribution and utilize the $\operatorname{softmax}$ output activation as in supervised classification.

(State-) Value and Action-Value Functions



To evaluate a quality of a policy, we define value function $v_{\pi}(s)$, or state-value function, as

$$egin{aligned} v_{\pi}(s) &\stackrel{ ext{def}}{=} \mathbb{E}_{\pi}\left[G_{t} | S_{t} = s
ight] = \mathbb{E}_{\pi}\left[\sum_{k=0}^{\infty} \gamma^{k} R_{t+k+1} \middle| S_{t} = s
ight] \ &= \mathbb{E}_{A_{t} \sim \pi(s)} \mathbb{E}_{S_{t+1}, R_{t+1} \sim p(s, A_{t})} ig[R_{t+1} + \gamma \mathbb{E}_{A_{t+1} \sim \pi(S_{t+1})} \mathbb{E}_{S_{t+2}, R_{t+2} \sim p(S_{t+1}, A_{t+1})} ig[R_{t+2} + \dots ig] ig] \end{aligned}$$

An action-value function for a policy π is defined analogously as

$$q_\pi(s,a) \stackrel{ ext{ iny def}}{=} \mathbb{E}_\pi \left[G_t | S_t = s, A_t = a
ight] = \mathbb{E}_\pi \left[\sum_{k=0}^\infty \gamma^k R_{t+k+1} \middle| S_t = s, A_t = a
ight].$$

The value function and the state-value function can be easily expressed using one another:

$$v_\pi(s)=\mathbb{E}_{a\sim\pi}ig[q_\pi(s,a)ig],$$
 elimination, joe to inhart z definice inhart. $q_\pi(s,a)=\mathbb{E}_{s',r\sim p}ig[r+\gamma v_\pi(s')ig].$ record z_π to byth dostal i nown strum way which

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RL

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Optimal Value Functions



Optimal state-value function is defined as

$$v_*(s) \stackrel{ ext{ iny def}}{=} \max_{\pi} v_{\pi}(s),$$

and optimal action-value function is defined analogously as

$$q_*(s,a) \stackrel{ ext{ iny def}}{=} \max_{\pi} q_{\pi}(s,a).$$

Any policy π_* with $v_{\pi_*}=v_*$ is called an **optimal policy**. Such policy can be defined as $\pi_*(s)\stackrel{\text{def}}{=} rg \max_a q_*(s,a) = rg \max_a \mathbb{E}[R_{t+1}+\gamma v_*(S_{t+1})|S_t=s,A_t=a]$. When multiple actions maximize $q_*(s,a)$, the optimal policy can stochastically choose any of them.

Existence

In finite-horizon tasks or if $\gamma < 1$, there always exists a unique optimal state-value function, a unique optimal action-value function, and a (not necessarily unique) optimal policy.

Policy Gradient Methods



We train the policy

$$\pi(a|s;m{ heta})$$

by maximizing the expected return $v_{\pi}(s)$.

To that account, we need to compute its **gradient** $\nabla_{\theta} v_{\pi}(s)$.

Policy Gradient Theorem



Assume that ${\mathcal S}$ and ${\mathcal A}$ are finite, $\gamma=1$, and that maximum episode length H is also finite.

Let $\pi(a|s; \boldsymbol{\theta})$ be a parametrized policy. We denote the initial state distribution as h(s) and the on-policy distribution under π as $\mu(s)$. Let also $J(\boldsymbol{\theta}) \stackrel{\text{def}}{=} \mathbb{E}_{s \sim h} v_{\pi}(s)$.

Then

$$abla_{m{ heta}} v_{\pi}(s) \propto \sum_{s' \in \mathcal{S}} P(s
ightarrow \ldots
ightarrow s' | \pi) \sum_{a \in \mathcal{A}} q_{\pi}(s',a)
abla_{m{ heta}} \pi(a|s';m{ heta})$$

C> past, juh casto se dostníny do stana s

and

$$abla_{m{ heta}} J(m{ heta}) \propto \sum_{s \in \mathcal{S}} \mu(s) \sum_{a \in \mathcal{A}} q_{\pi}(s,a)
abla_{m{ heta}} \pi(a|s;m{ heta}),$$

where $P(s \to ... \to s' | \pi)$ is the probability of getting to state s' when starting from state s, after any number of 0, 1, ... steps.

Proof of Policy Gradient Theorem



$$egin{align*}
abla v_{\pi}(s) &=
abla \Big[\sum_{a} \pi(a|s;oldsymbol{ heta}) q_{\pi}(s,a) \Big] \ &= \sum_{a} \Big[q_{\pi}(s,a)
abla \pi(a|s;oldsymbol{ heta}) + \pi(a|s;oldsymbol{ heta})
abla q_{\pi}(s,a) \Big] ext{jectur interalise} \ &= \sum_{a} \Big[q_{\pi}(s,a)
abla \pi(a|s;oldsymbol{ heta}) + \pi(a|s;oldsymbol{ heta})
abla \Big(\sum_{s',r} p(s',r|s,a)(r+v_{\pi}(s')) \Big) \Big] \ &= \sum_{a} \Big[q_{\pi}(s,a)
abla \pi(a|s;oldsymbol{ heta}) + \pi(a|s;oldsymbol{ heta}) \Big(\sum_{s',r} p(s'|s,a)
abla v_{\pi}(s') \Big) \Big] \end{aligned}$$

We now expand $v_{\pi}(s')$.

$$=\sum_{a}\left[q_{\pi}(s,a)
abla\pi(a|s;oldsymbol{ heta})+\pi(a|s;oldsymbol{ heta})\Big(\sum_{s'}p(s'|s,a)\Big(\sum_{s''}p(s''|s',a')
abla\pi(a'|s';oldsymbol{ heta})+\pi(a'|s';oldsymbol{ heta})\Big(\sum_{s''}p(s''|s',a')
ablavour_{\pi}(s'')\Big)\Big]\Big)\Big)\Big]$$

Continuing to expand all $v_{\pi}(s'')$, we obtain the following:

$$abla v_\pi(s) = \sum_{s' \in \mathcal{S}} \sum_{k=0}^H P(s o s' ext{ in } k ext{ steps } | \pi) \sum_{a \in \mathcal{A}} q_\pi(s', a)
abla_{oldsymbol{ heta}} \pi(a|s'; oldsymbol{ heta}).$$

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Proof of Policy Gradient Theorem



To finish the proof of the first part, it is enough to realize that

$$\sum
olimits_{k=0}^H P(s o s' ext{ in } k ext{ steps } |\pi) \propto P(s o \ldots o s' |\pi).$$

For the second part, we know that

$$abla_{m{ heta}} J(m{ heta}) = \mathbb{E}_{s\sim h}
abla_{m{ heta}} v_{\pi}(s) \propto \mathbb{E}_{s\sim h} \sum_{s'\in\mathcal{S}} P(s
ightarrow \ldots
ightarrow s'|\pi) \sum_{a\in\mathcal{A}} q_{\pi}(s',a)
abla_{m{ heta}} \pi(a|s';m{ heta}),$$

therefore using the fact that $\mu(s') = \mathbb{E}_{s \sim h} P(s
ightarrow \ldots
ightarrow s' | \pi)$ we get

$$abla_{m{ heta}} J(m{ heta}) \propto \sum_{s \in S} \mu(s) \sum_{a \in A} q_{\pi}(s,a)
abla_{m{ heta}} \pi(a|s;m{ heta}).$$

Finally, note that the theorem can be proven with infinite S and A; and also for infinite episodes when discount factor $\gamma < 1$.

NAS

REINFORCE Algorithm



The REINFORCE algorithm (Williams, 1992) uses directly the policy gradient theorem, minimizing $-J(\boldsymbol{\theta}) \stackrel{\text{def}}{=} -\mathbb{E}_{s\sim h} v_{\pi}(s)$. The loss gradient is then $\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}$

$$abla_{m{ heta}} - J(m{ heta}) \propto -\sum_{s \in \mathcal{S}} \mu(s) \sum_{a \in \mathcal{A}} q_{\pi}(s,a)
abla_{m{ heta}} \pi(a|s;m{ heta}) = \mathbb{E}_{s \sim \mu} \sum_{a \in \mathcal{A}} q_{\pi}(s,a)
abla_{m{ heta}} \pi(a|s;m{ heta}).$$

However, the sum over all actions is problematic. Instead, we rewrite it to an expectation which we can estimate by sampling:

$$abla_{m{ heta}} - J(m{ heta}) \propto \mathbb{E}_{s \sim \mu} \mathbb{E}_{a \sim \pi} q_{\pi}(s, a)
abla_{m{ heta}} - \log \pi(a|s; m{ heta}),$$

where we used the fact that

$$abla_{m{ heta}} \log \pi(a|s;m{ heta}) = rac{1}{\pi(a|s;m{ heta})}
abla_{m{ heta}} \pi(a|s;m{ heta}).$$

REINFORCE Algorithm



REINFORCE therefore minimizes the loss $-J(\theta)$ with gradient and the start of the

$$\mathbb{E}_{s\sim\mu}\mathbb{E}_{a\sim\pi}q_{\pi}(s,a)
abel json realize to, we chief policy $\mathbb{E}_{s\sim\mu}\mathbb{E}_{a\sim\pi}q_{\pi}(s,a)
abel json realize ale to, we chief policy $\mathbb{E}_{s\sim\mu}\mathbb{E}_{a\sim\pi}q_{\pi}(s,a)
abel json realize ale to, we chief policy $\pi(a|s;m{ heta}),$$$$$

where we estimate the $q_{\pi}(s,a)$ by a single sample.

Note that the loss is just a weighted variant of negative log-likelihood (NLL), where the sampled actions play a role of gold labels and are weighted according to their return.

REINFORCE: Monte-Carlo Policy-Gradient Control (episodic) for π_*

Input: a differentiable policy parameterization $\pi(a|s, \theta)$

Algorithm parameter: step size $\alpha > 0$

Initialize policy parameter $\boldsymbol{\theta} \in \mathbb{R}^{d'}$ (e.g., to 0)

Loop forever (for each episode):

Generate an episode $S_0, A_0, R_1, \ldots, S_{T-1}, A_{T-1}, R_T$, following $\pi(\cdot|\cdot, \boldsymbol{\theta})$

Loop for each step of the episode t = 0, 1, ..., T - 1:

$$G \leftarrow \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k$$

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha G \nabla \ln \pi (A_t | S_t, \boldsymbol{\theta})$$

Modified from Algorithm 13.3 of "Reinforcement Learning: An Introduction", http://www.incompleteideas.net/book/the-book-2nd.html by removing γˆt from the update of θ

 (G_t)

REINFORCE Algorithm Example Performance



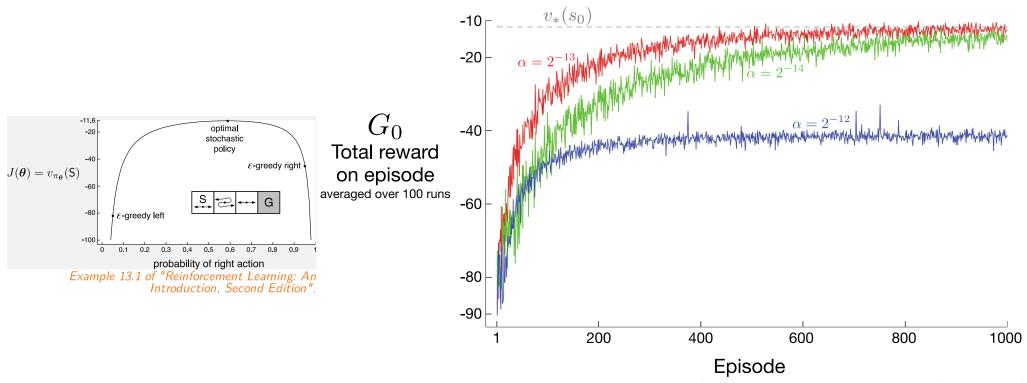


Figure 13.1 of "Reinforcement Learning: An Introduction, Second Edition".

REINFORCE with Baseline



The returns can be arbitrary – better-than-average and worse-than-average returns cannot be recognized from the absolute value of the return.

Hopefully, we can generalize the policy gradient theorem using a baseline b(s) to

$$abla_{m{ heta}}J(m{ heta}) \propto \sum_{s \in \mathcal{S}} \mu(s) \sum_{a \in \mathcal{A}} \left(q_{\pi}(s,a) - b(s)
ight)
abla_{m{ heta}} \pi(a|s;m{ heta}).$$

The baseline b(s) can be a function or even a random variable, as long as it does not depend on a, because $\int d^2 h \, dz$, $\bar{z}e$ je fe imann' we of offsets

$$\sum_{a} \widehat{b(s)} \overline{
abla_{m{ heta}} \pi(a|s;m{ heta})} = b(s) \sum_{a} \overline{
abla_{m{ heta}} \pi(a|s;m{ heta})} = b(s) \overline{
abla_{m{ heta}} \pi(a|s;m{ heta})} = 0.$$

Porovinjume aher proti prémieure hodusté ~ value function

REINFORCE with Baseline



A good choice for b(s) is $v_{\pi}(s)$, which can be shown to minimize the variance of the gradient estimator. Such baseline reminds centering of the returns, given that

$$v_\pi(s) = \mathbb{E}_{a \sim \pi} q_\pi(s,a).$$

Then, better-than-average returns are positive and worse-than-average returns are negative.

The resulting $q_{\pi}(s,a)-v_{\pi}(s)$ function is also called the **advantage** function

$$a_\pi(s,a) \stackrel{ ext{ iny def}}{=} q_\pi(s,a) - v_\pi(s).$$

Of course, the $v_{\pi}(s)$ baseline can be only approximated. If neural networks are used to estimate $\pi(a|s;\boldsymbol{\theta})$, then some part of the network is usually shared between the policy and value function estimation, which is trained using mean square error of the predicted and observed return.

MDP

REINFORCE with Baseline



REINFORCE with Baseline (episodic), for estimating $\pi_{\theta} \approx \pi_*$

Input: a differentiable policy parameterization $\pi(a|s, \theta)$

Input: a differentiable state-value function parameterization $\hat{v}(s, \mathbf{w})$

Algorithm parameters: step sizes $\alpha^{\theta} > 0$, $\alpha^{\mathbf{w}} > 0$

Initialize policy parameter $\boldsymbol{\theta} \in \mathbb{R}^{d'}$ and state-value weights $\mathbf{w} \in \mathbb{R}^{d}$ (e.g., to $\mathbf{0}$)

Loop forever (for each episode):

Generate an episode $S_0, A_0, R_1, \ldots, S_{T-1}, A_{T-1}, R_T$, following $\pi(\cdot|\cdot, \boldsymbol{\theta})$

Loop for each step of the episode $t = 0, 1, \dots, T-1$:

$$G \leftarrow \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k$$

$$\delta \leftarrow G - \left[\hat{v}(S_t, \mathbf{w}) \right] \longrightarrow \text{ jak join after primeric doby'}$$

$$\mathbf{w} \leftarrow \mathbf{w} + \alpha^{\mathbf{w}} \delta \nabla \hat{v}(S_t, \mathbf{w}) \longrightarrow \text{ ten primer si hids trehant}$$

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha^{\boldsymbol{\theta}} \delta \nabla \ln \pi (A_t | S_t, \boldsymbol{\theta})$$

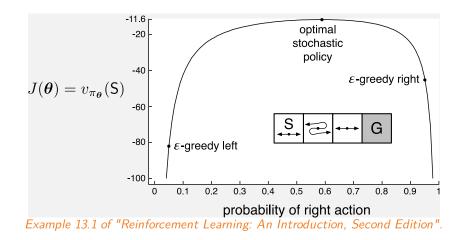
Modified from Algorithm 13.4 of "Reinforcement Learning: An Introduction", http://www.incompleteideas.net/book/the-book-2nd.html by removing γ from the update of θ

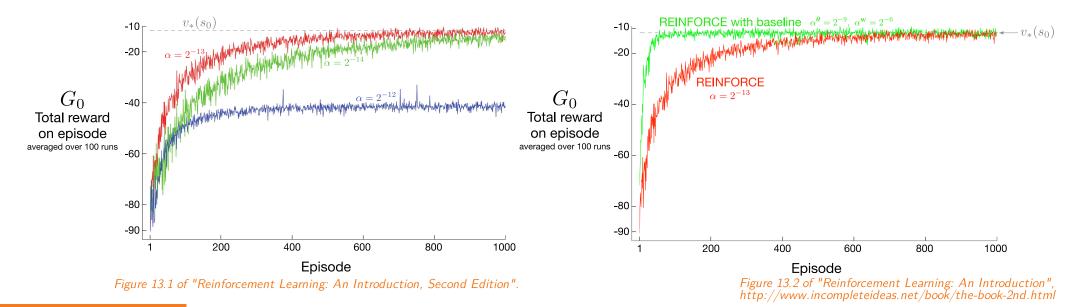
VAF

 (G_t)

REINFORCE with Baseline Example Performance







NPFL138, Lecture 12 RL MABandits MDP REINFORCE Baseline NAS RLWhatNext Generative Models VAE 27/56



- We can design neural network architectures using reinforcement learning.
- The designed network is encoded as a sequence of elements, and is generated using an RNN controller, which is trained using the REINFORCE with baseline algorithm.

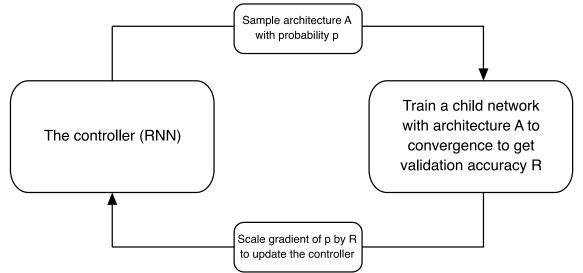


Figure 1 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

• For every generated sequence, the corresponding network is trained on CIFAR-10 and the development accuracy is used as a return.



The overall architecture of the designed network is fixed and only the Normal Cells and Reduction Cells are generated by the controller.

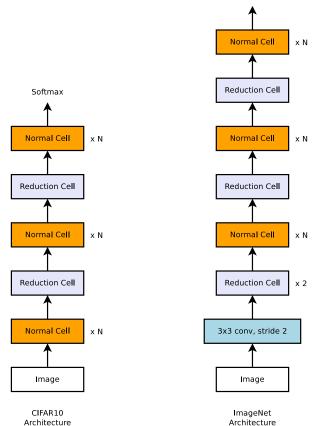


Figure 2 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

Softmax



- Each cell is composed of B blocks (B=5 is used in NASNet).
- Each block is designed by a RNN controller generating 5 parameters.

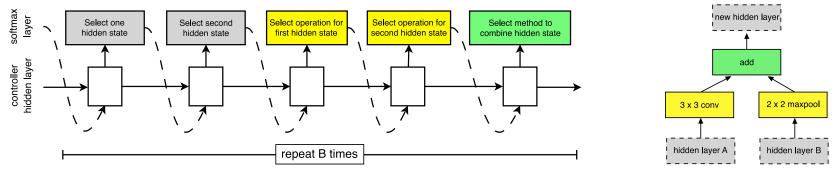


Figure 3. Controller model architecture for recursively constructing one block of a convolutional cell. Each block requires selecting 5 discrete parameters, each of which corresponds to the output of a softmax layer. Example constructed block shown on right. A convolutional cell contains B blocks, hence the controller contains 5B softmax layers for predicting the architecture of a convolutional cell. In our experiments, the number of blocks B is 5.

Figure 3 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

- **Step 1.** Select a hidden state from h_i, h_{i-1} or from the set of hidden states created in previous blocks.
- **Step 2.** Select a second hidden state from the same options as in Step 1.
- **Step 3.** Select an operation to apply to the hidden state selected in Step 1.
- **Step 4.** Select an operation to apply to the hidden state selected in Step 2.
- **Step 5.** Select a method to combine the outputs of Step 3 and 4 to create

Page 3 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

- identity
- 1x7 then 7x1 convolution
- 3x3 average pooling
- 5x5 max pooling
- 1x1 convolution
- 3x3 depthwise-separable conv
- 7x7 depthwise-separable conv

- 1x3 then 3x1 convolution
- 3x3 dilated convolution
- 3x3 max pooling
- 7x7 max pooling
- 3x3 convolution
- 5x5 depthwise-seperable conv

Figure 2 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

NPFL138. Lecture 12

MABandits

Baseline

NAS

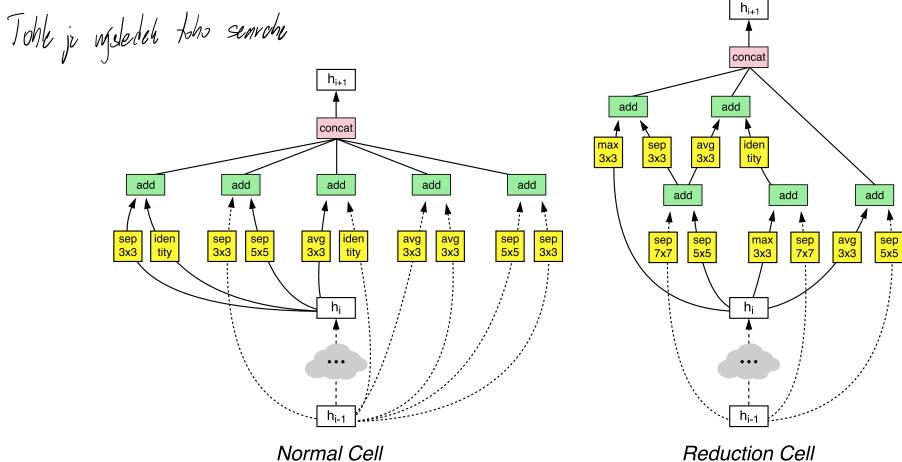
RLWhatNext

30/56

VAF



The final Normal Cell and Reduction Cell chosen from 20k architectures (500GPUs, 4days).



Page 3 of "Learning Transferable Architectures for Scalable Image Recognition", https://arxiv.org/abs/1707.07012

EfficientNet Search



EfficientNet changes the search in three ways.

ullet Computational requirements are part of the return. Notably, the goal is to find an architecture m maximizing

$$\text{DevelopmentAccuracy}(m) \cdot \left(\frac{\text{TargetFLOPS}{=400\text{M}}}{\text{FLOPS}(m)}\right)^{0.07},$$

where the constant 0.07 balances the accuracy and FLOPS (the constant comes from an empirical observation that doubling the FLOPS brings about 5% relative accuracy gain, and $1.05=2^{\beta}$ gives $\beta\approx 0.0704$).

- It uses a different search space allowing to control kernel sizes and channels in different parts of the architecture (compared to using the same cell everywhere as in NASNet).
- Training directly on ImageNet, but only for 5 epochs.

In total, 8k model architectures are sampled, and PPO algorithm is used instead of the REINFORCE with baseline.

EfficientNet Search



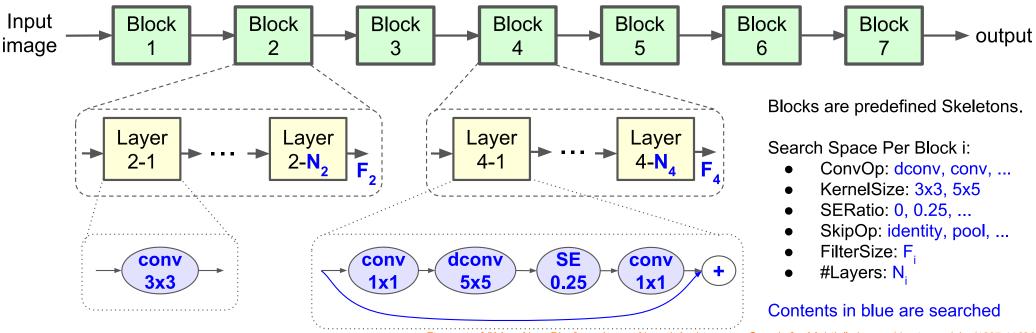


Figure 4 of "MnasNet: Platform-Aware Neural Architecture Search for Mobile", https://arxiv.org/abs/1807.11626

The overall architecture consists of 7 blocks, each described by 6 parameters – 42 parameters in total, compared to 50 parameters of Convolutional kernel size Kernel Size: 3x3, 5x5. the NASNet search space.

- Convolutional ops ConvOp: regular conv (conv), depthwise conv (dconv), and mobile inverted bottleneck conv [29].
- Squeeze-and-excitation [13] ratio SERatio: 0, 0.25.
- Skip ops SkipOp: pooling, identity residual, or no skip.
- Output filter size F_i .
- Number of layers per block N_i .

Page 4 of "MnasNet: Platform-Aware Neural Architecture Search for Mobile" https://arxiv.org/abs/1807.11626

EfficientNet-B0 Baseline Network



Stage i	Operator $\hat{\mathcal{F}}_i$	Resolution $\hat{H}_i imes \hat{W}_i$	#Channels \hat{C}_i	\hat{L}_i #Layers
1	Conv3x3	224×224	32	1
2	MBConv1, k3x3	112×112	16	1
3	MBConv6, k3x3	112×112	24	2
4	MBConv6, k5x5	56×56	40	2
5	MBConv6, k3x3	28×28	80	3
6	MBConv6, k5x5	14×14	112	3
7	MBConv6, k5x5	14×14	192	4
8	MBConv6, k3x3	7×7	320	1
9	Conv1x1 & Pooling & FC	7×7	1280	1

Table 1 of "EfficientNet: Rethinking Model Scaling for Convolutional Neural Networks", https://arxiv.org/abs/1905.11946

What Next



If you liked the introduction to the deep reinforcement learning, I have a whole course NPFL139 – Deep Reinforcement Learning.

- It covers a range of reinforcement learning algorithms, from the basic ones to more advanced algorithms utilizing deep neural networks.
- Summer semester, 3/2 C+Ex, 8 e-credits, similar structure as Deep learning.
- An elective (povinně volitelný) course in the programs:
 - Artificial Intelligence,
 - Language Technologies and Computational Linguistics.

Generative Models



Generative Models

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Generative Models





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Generative Models



Everyone: AI art will make designers obsolete

Everyone: AI art will make designers obsolete

Al accepting the job:







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RL

Generative Models



Generative models are given a set of realizations of a random variable \mathbf{x} and their goal is to estimate $P(\mathbf{x})$.

Usually the goal is to be able to sample from $P(\mathbf{x})$, but sometimes an explicit calculation of $P(\mathbf{x})$ is also possible.

Deep Generative Models



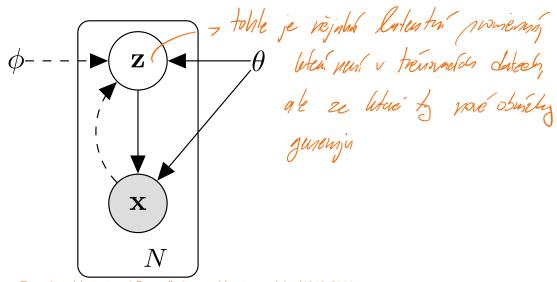


Figure 1 of "Auto-Encoding Variational Bayes", https://arxiv.org/abs/1312.6114

One possible approach to estimate $P(m{x})$ is to assume that the random variable $m{x}$ depends on a the its trenant unine latent variable z:

$$P(oldsymbol{x}) = \sum_{oldsymbol{z}} P(oldsymbol{z}) P(oldsymbol{x} | oldsymbol{z}) = \mathbb{E}_{oldsymbol{z} \sim P(oldsymbol{z})} P(oldsymbol{x} | oldsymbol{z}).$$

We use neural networks to estimate the conditional probability $P_{\theta}(x|z)$.

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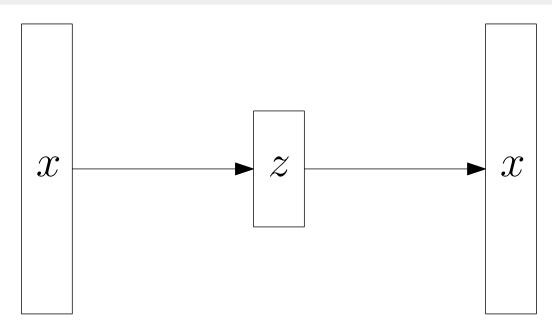
RLWhatNext

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AutoEncoders

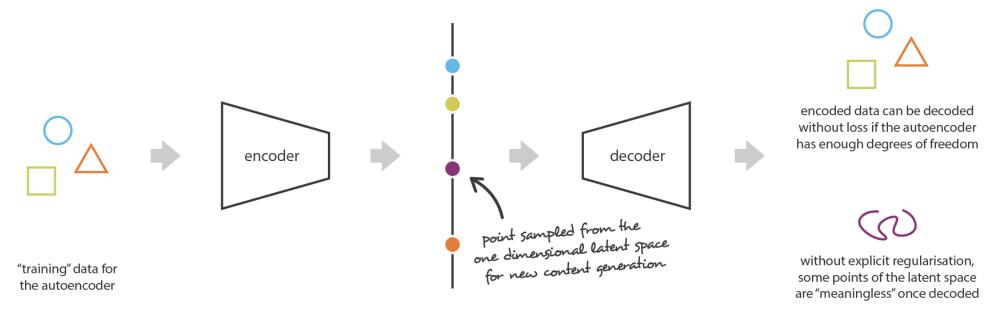




- Autoencoders are useful for unsupervised feature extraction, especially when performing input compression (i.e., when the dimensionality of the latent space z is smaller than the dimensionality of the input).
- ullet When $oldsymbol{x}+oldsymbol{arepsilon}$ is used as input, autoencoders can perform denoising.
- ullet However, the latent space $m{z}$ does not need to be fully covered, so a randomly chosen $m{z}$ does not need to produce a valid $m{x}$.

AutoEncoders





https://miro.medium.com/max/3608/1*iSfaVxcGi_ELkKgAG0YRlQ@2x.png



We assume $P(\mathbf{z})$ is fixed and independent on \mathbf{x} .

We approximate $P(\boldsymbol{x}|\boldsymbol{z})$ using $P_{\boldsymbol{\theta}}(\boldsymbol{x}|\boldsymbol{z})$. However, in order to train an autoencoder, we need to know the posterior $P_{\boldsymbol{\theta}}(\boldsymbol{z}|\boldsymbol{x})$, which is usually intractable.

We therefore approximate $P_{\boldsymbol{\theta}}(\boldsymbol{z}|\boldsymbol{x})$ by a trainable $Q_{\boldsymbol{\varphi}}(\boldsymbol{z}|\boldsymbol{x})$.

Jensen's Inequality



To derive a loss for training variational autoencoders, we first formulate the Jensen's inequality.

Recall that convex functions by definition fulfil that for ${m u}, {m v}$ and real $0 \le t \le 1$,

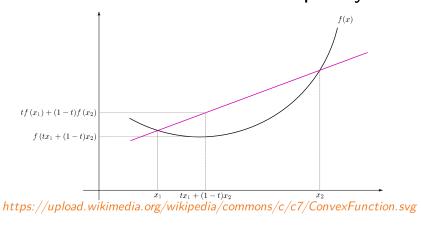
$$f(toldsymbol{u}+(1-t)oldsymbol{v})\leq tf(oldsymbol{u})+(1-t)f(oldsymbol{v}).$$

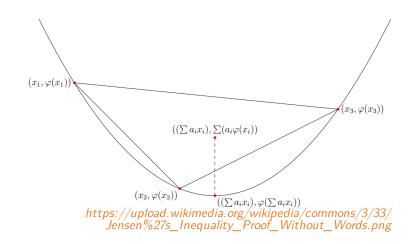
The **Jensen's inequality** generalizes the above property to any *convex* combination of points: if we have $u_i \in \mathbb{R}^D$ and https://upload.wikimedia.org/wikipedia/commons/c/c7/ConvexFunction.svg weights $w_i \in \mathbb{R}^+$ such that $\sum_i w_i = 1$, it holds that

$$fig(\sum_i w_i oldsymbol{u}_iig) \leq \sum_i w_i fig(oldsymbol{u}_iig).$$

The Jensen's inequality can be formulated also for probability distributions (whose expectation can be considered an infinite convex combination):

$$fig(\mathbb{E}[\mathbf{u}]ig) \leq \mathbb{E}_{\mathbf{u}}ig[f(\mathbf{u})ig].$$





VAE – Loss Function Derivation



Our goal will be to maximize the log-likelihood as usual, but we need to express it using the latent variable **z**:

$$\log P_{m{ heta}}(m{x}) = \log \mathbb{E}_{P(m{z})} ig[P_{m{ heta}}(m{x}|m{z}) ig].$$

However, approximating the expectation using a single sample has monstrous variance, because for most \boldsymbol{z} , $P_{\boldsymbol{\theta}}(\boldsymbol{x}|\boldsymbol{z})$ will be nearly zero.

We therefore turn to our *encoder*, which is able for a given
$$\boldsymbol{x}$$
 to generate "its" \boldsymbol{z} :
$$\log P_{\boldsymbol{\theta}}(\boldsymbol{x}) = \log \mathbb{E}_{P(\boldsymbol{z})} \left[P_{\boldsymbol{\theta}}(\boldsymbol{x}|\boldsymbol{z}) \right] \cdot \frac{Q_{\mathcal{A}}(\boldsymbol{z}|\boldsymbol{x})}{Q_{\mathcal{A}}(\boldsymbol{z}|\boldsymbol{x})} \right]$$

$$= \log \mathbb{E}_{Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})} \left[P_{\boldsymbol{\theta}}(\boldsymbol{x}|\boldsymbol{z}) \cdot \frac{P(\boldsymbol{z})}{Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})} \right]$$

$$\geq \mathbb{E}_{Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})} \left[\log P_{\boldsymbol{\theta}}(\boldsymbol{x}|\boldsymbol{z}) + \log \frac{P(\boldsymbol{z})}{Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})} \right]$$

proble ve nesamply uplik while $=\frac{\mathbb{E}_{Q_{\varphi}(m{z}|m{x})}\left[\log P_{m{ heta}}(m{x}|m{z})
ight]}{2}-D_{\mathrm{KL}}\left(Q_{\varphi}(m{z}|m{x})\|P(m{z})
ight).$ jeste the PL138, Lecture 12 RL MARANDITE.

VAE – Variational (or Evidence) Lower Bound



The resulting variational lower bound or evidence lower bound (ELBO), denoted $\mathcal{L}(\theta, \varphi; \mathbf{x})$, can be also defined explicitly as:

$$\mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) = \log P_{oldsymbol{ heta}}(oldsymbol{x}) - D_{\mathrm{KL}}ig(Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x}) \|P_{oldsymbol{ heta}}(oldsymbol{z}|oldsymbol{x})ig).$$

Because KL-divergence is nonnegative, $\mathcal{L}(\boldsymbol{\theta}, \boldsymbol{\varphi}; \mathbf{x}) \leq \log P_{\boldsymbol{\theta}}(\boldsymbol{x})$.

By using simple properties of conditional and joint probability, we get that

$$egin{aligned} \mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) &= \mathbb{E}_{Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})} igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}) + \log P_{oldsymbol{ heta}}(oldsymbol{z}|oldsymbol{x}) - \log Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x}) igg] \ &= \mathbb{E}_{Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})} igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z}) + \log P(oldsymbol{z}) - \log Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x}) igg] \ &= \mathbb{E}_{Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})} igg[\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z}) igg] - D_{\mathrm{KL}}ig(Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x}) \|P(oldsymbol{z}) igg). \end{aligned}$$

Variational AutoEncoders Training



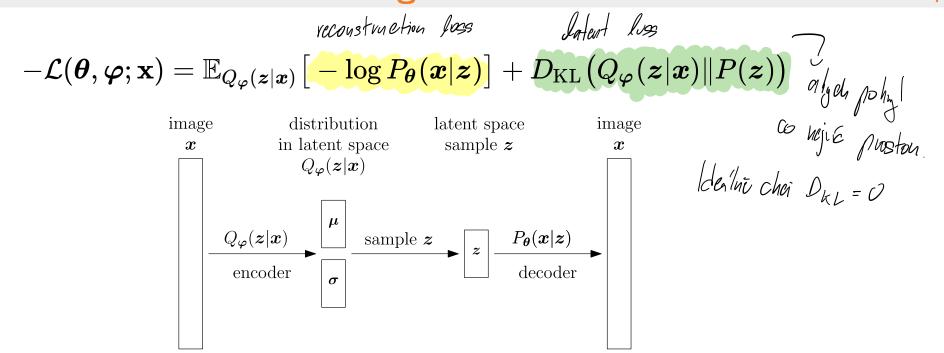
$$-\mathcal{L}(oldsymbol{ heta},oldsymbol{arphi};\mathbf{x}) = \mathbb{E}_{Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})}ig[-\log P_{oldsymbol{ heta}}(oldsymbol{x}|oldsymbol{z})ig] + D_{\mathrm{KL}}ig(Q_{oldsymbol{arphi}}(oldsymbol{z}|oldsymbol{x})\|P(oldsymbol{z})ig)$$

- We train a VAE by minimizing the $-\mathcal{L}(\boldsymbol{\theta}, \boldsymbol{\varphi}; \mathbf{x})$.
- The $\mathbb{E}_{Q_{\omega}(\boldsymbol{z}|\boldsymbol{x})}$ is estimated using a single sample.
- The distribution $Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})$ is parametrized as a normal distribution $\mathcal{N}(\boldsymbol{z}|\boldsymbol{\mu},\boldsymbol{\sigma}^2)$, with the model predicting μ and σ given x.
 - In order for σ to be positive, we can use \exp activation function (so that the network predicts $\log \sigma$ before the activation), or for example a softplus activation function.
 - The normal distribution is used, because we can sample from it efficiently, we can backpropagate through it and we can compute D_{KL} analytically; furthermore, if we decide to parametrize $Q_{m{arphi}}(m{z}|m{x})$ using mean and variance, the maximum entropy principle suggests we should use the normal distribution.
- ullet We use a prior $P(oldsymbol{z}) = \mathcal{N}(oldsymbol{0}, oldsymbol{I}).$

MDP

Variational AutoEncoders Training





Note that the loss has 2 intuitive components:

- reconstruction loss starting with x, passing though Q_{φ} , sampling z and then passing through P_{θ} should arrive back at x;
- latent loss over all \boldsymbol{x} , the distribution of $Q_{\varphi}(\boldsymbol{z}|\boldsymbol{x})$ should be as close as possible to the prior $P(\boldsymbol{z}) = \mathcal{N}(\boldsymbol{0}, \boldsymbol{I})$, which is independent on \boldsymbol{x} .

Variational AutoEncoders – Reparametrization Trick



In order to backpropagate through $m{z} \sim Q_{m{arphi}}(m{z}|m{x})$, note that if

$$oldsymbol{z} \sim \mathcal{N}(oldsymbol{\mu}, oldsymbol{\sigma}^2),$$

we can write z as

the je shily, protoir to nem' inder; parametry

$$oldsymbol{z} \sim oldsymbol{\mu} + oldsymbol{\sigma} \odot \overline{\mathcal{N}(oldsymbol{0}, oldsymbol{I})}.$$

Such formulation then allows differentiating z with respect to μ and σ and is called a reparametrization trick (Kingma and Welling, 2013).

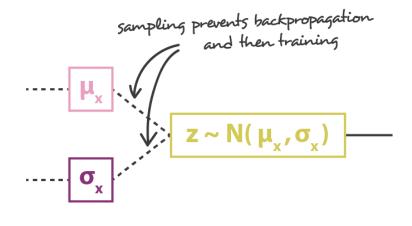
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Variational AutoEncoders – Reparametrization Trick

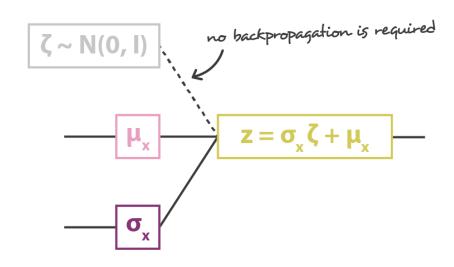


no problem for backpropagation

backpropagation is not possible due to sampling



sampling without reparametrisation trick



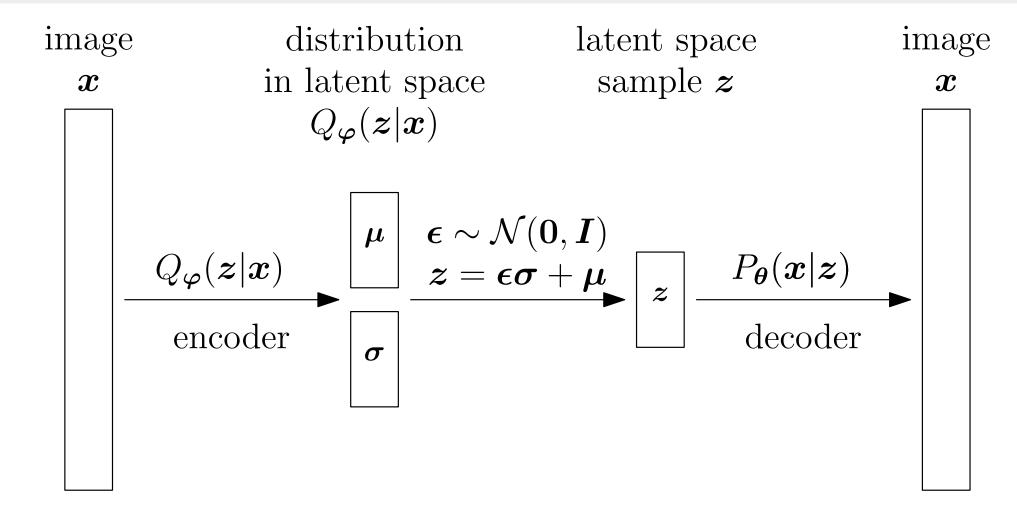
sampling with reparametrisation trick

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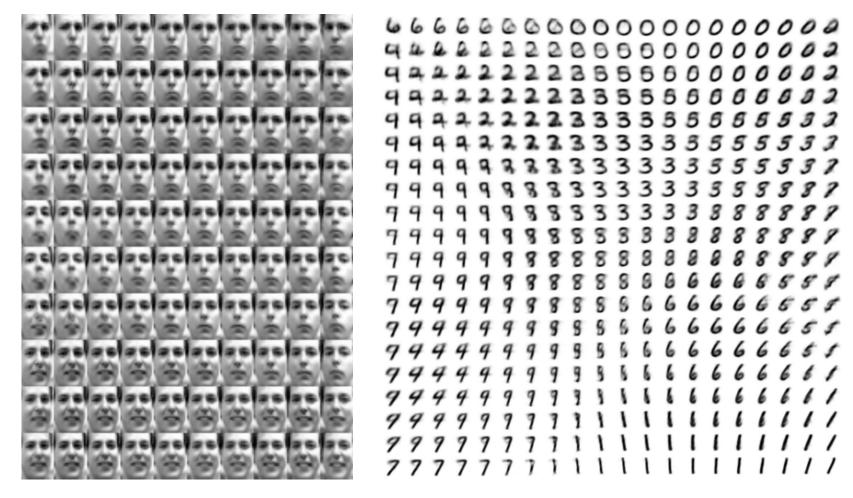
MDP

Variational AutoEncoders – Reparametrization Trick







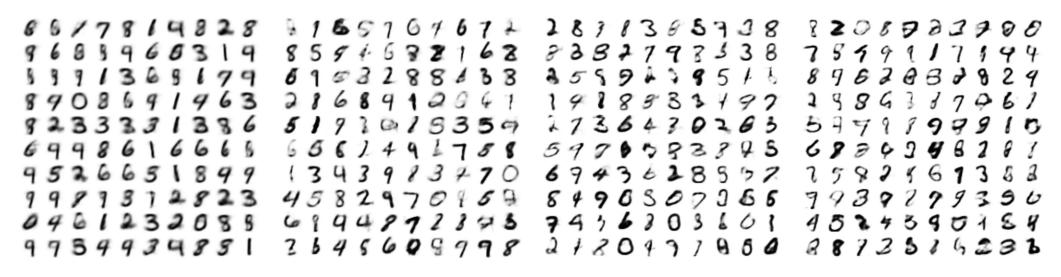


(a) Learned Frey Face manifold

(b) Learned MNIST manifold

Figure 4 of "Auto-Encoding Variational Bayes", https://arxiv.org/abs/1312.6114



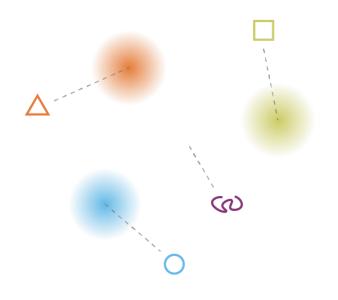


- (a) 2-D latent space
- (b) 5-D latent space
- (c) 10-D latent space
- (d) 20-D latent space

Figure 5 of "Auto-Encoding Variational Bayes", https://arxiv.org/abs/1312.6114

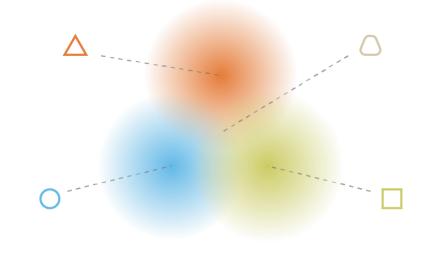
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what can happen without regularisation







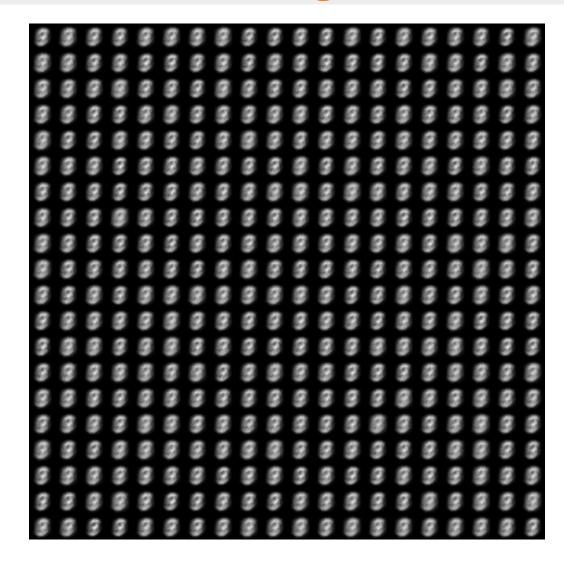
what we want to obtain with regularisation

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Variational AutoEncoders – Too High Latent Loss







Variational AutoEncoders – Too High Reconstruction Loss



