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# Structured Prediction, CTC, Word2Vec

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unless otherwise stated



# **Structured Prediction**

Span Labeling CTC

CTCDecoding

Word2Vec

CLEs

ELMo

#### **Structured Prediction**



Consider generating a sequence of  $y_1,\ldots,y_N\in\mathcal{Y}^N$  given input  $oldsymbol{x}_1,\ldots,oldsymbol{x}_N$ .

Predicting each sequence element independently models the distribution  $P(y_i | \boldsymbol{X})$ .



However, there may be dependencies among the  $y_i$  themselves, in the sense that not all sequences of  $y_i$  are valid; but when generating each  $y_i$  independently, the model might not be capable of generating only valid sequences.

#### **Structured Prediction – Span Labeling**

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Consider for example **named entity recognition**, whose goal is to locate *named entities*, which are single words or sequences of multiple words denoting real-world objects, concepts, and events. The most common types of named entities include:

- PER: *people*, including names of individuals, historical figures, and even fictional characters;
- ORG: *organizations*, incorporating companies, government agencies, educational institutions, and others;
- LOC: *locations*, encompassing countries, cities, geographical features, addresses.

Compared to part-of-speech tagging, locating named entities is much more challenging – named entity mentions are generally multi-word spans, and arbitrary number of named entities can appear in a sentence (consequently, we cannot use accuracy for evaluation; F1-score is commonly used). *Qecumay hyph nemel public cemu hodno hit* Named entity recognition is an instance of a **span labeling** task, where the goal is to locate and classify spans in the input sequence.

#### Span Labeling – BIO Encoding

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A possible approach to a span labeling task is to classify every sequence element using a specialized tag set. A common approach is to use the **BIO** encoding, which consists of

- 0: *outside*, the given element is not part of any span;
- B-PER, B-ORG, B-LOC, ...: *beginning*, the element is first in a new span;
- I-PER, I-ORG, I-LOC, ...: *inside*, a continuation element of an existing span.

✓In a valid sequence, the I-TYPE must follow either B-TYPE or I-TYPE.

(Formally, the described scheme is IOB-2 format; there exists quite a few other possibilities like IOB-1, IEO, BILOU, ...)

The described encoding can represent any set of continuous typed spans (when no spans overlap, i.e., a single element can belong to at most one span).

OBIIIO - tulkke hy byla zahísdovaní dyřslovní sehvenec

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#### Span Labeling – BIO Encoding

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However, when predicting each of the element tags independently, invalid sequences might be created.

- We can decide to ignore it and use heuristics capable of recovering the spans from invalid sequences of BIO tags.
- We can employ a decoding algorithm producing the most probable **valid sequence** of tags during prediction.
  - However, during training we do not consider the BIO tags validity.
- We might use a different loss enabling the model to consider only valid BIO tag sequences also during training.

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ELMo

#### **Span Labeling – Decoding Algorithm**



Let  $\boldsymbol{x}_1, \ldots, \boldsymbol{x}_N$  be an input sequence.

Our goal is to produce an output sequence  $y_1,\ldots,y_N$ , where each  $y_t\in\mathcal{Y}$  with Y classes.

Assume we have a model predicting  $p(y_t = k | \mathbf{X}; \boldsymbol{\theta})$ , a probability that the *t*-th output element  $y_t$  is the class k. However, only some sequences  $\boldsymbol{y}$  are valid. We now make an assumption that the validity of a

However, only some sequences y are valid. We now make an assumption that the validity of a sequence depends only on the validity of **neighboring** output classes. In other words, if all neighboring pairs of output elements are valid, the whole sequence is.

- The validity of neighboring pairs can be described by a transition matrix  $oldsymbol{A} \in \{0,1\}^{Y imes Y}$ .
- Such an approach allows expressing the (in)validity of a BIO tag sequence.
  - However, the current formulation does not enforce conditions on the first and the last tag.

If needed (for example to disallow I-TYPE as the first tag), we can add fixed  $y_0$  and/or  $y_{N+1}$  imposing conditions on  $y_1$  and/or  $y_N$ , respectively.

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#### **Span Labeling – Decoding Algorithm**

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Let us denote  $\alpha_t(k)$  the log probability of the most probable output sequence of t elements with the last one being k.

We can compute  $\alpha_t(k)$  efficiently using dynamic programming. The core idea is the following:



The resulting algorithm is also called the **Viterbi algorithm**, and it is also a search for the path of maximum length in an acyclic graph.

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#### **Span Labeling – Decoding Algorithm**

**Inputs**: Input sequence of length N, tag set with Y tags.

**Inputs**: Model computing  $p(y_t = k | \boldsymbol{X}; \boldsymbol{\theta})$ , a probability that  $y_t$  should have the class k. **Inputs**: Transition matrix  $\boldsymbol{A} \in \mathbb{R}^{Y \times Y}$  indicating valid and invalid transitions.

**Outputs**: The most probable sequence  $oldsymbol{y}$  consisting of valid transitions only.

Time Complexity:  $O(N \cdot Y^2)$  in the worst case. > Constmint - triple by by 1

- For t = 1, ..., N: • For k = 1, ..., Y: • For k = 1, ..., Y: •  $Cim vetsi polyninky, tim pomulejs(...) <math>O(N \cdot Y^3)$ ...
  - $\alpha_t(k) \leftarrow \log p(y_t = k | \boldsymbol{X}; \boldsymbol{\theta})$  logits (unnormalized log probs) can also be used
  - If t > 1:  $\beta_t(k) \leftarrow \arg \max_{j, \text{ such that } A_{j,k} \text{ is valid } \alpha_{t-1}(j)$   $\alpha_t(k) \leftarrow \alpha_t(k) \leftarrow \alpha_t(k) \leftarrow \alpha_{t-1}(\beta_t(k))$ 
    - $lpha_t(k) \leftarrow lpha_t(k) + lpha_{t-1}ig(eta_t(k)ig)$
- The most probable sequence has the log probability  $\max \alpha_N$ , and its elements can be recovered by traversing  $\beta$  from t = N downto t = 1.

#### **Span Labeling – Other Approaches**

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With deep learning models, constrained decoding is usually sufficient to deliver high performance. Trennjeme , halabala, az interence houtaling podmintary Historically, there have been also other approaches:

#### • Maximum Entropy Markov Models

We might model the dependencies by explicitly conditioning on the previous label:

 $P(y_i|oldsymbol{X},y_{i-1}).$ 

Then, each label is predicted by a softmax from a hidden state and a previous label.



The decoding can still be performed by a dynamic programming algorithm.

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#### **Span Labeling – Other Approaches**

• Conditional Random Fields (CRF) - v christ dobé jour madely the silve, is not policha trivout In the simplest variant, Linear-chain CRF, usually abbreviated only to CRF, can be

In the simplest variant, Linear-chain CRF, usually abbreviated only to CRF, can be considered an extension of softmax – instead of a sequence of independent softmaxes, it is a sentence-level softmax, with additional weights for neighboring sequence elements.

We start by defining a score of a label sequence  $oldsymbol{y}$  as

$$s(oldsymbol{X},oldsymbol{y};oldsymbol{ heta},oldsymbol{A}) = f(y_1|oldsymbol{X};oldsymbol{ heta}) + \sum_{i=2}^Nig(oldsymbol{A}_{y_{i-1},y_i}+f(y_i|oldsymbol{X};oldsymbol{ heta})ig),$$

and define the probability of a label sequence  $oldsymbol{y}$  using  $\mathrm{softmax}$ :

of a label sequence 
$$\boldsymbol{y}$$
 using softmax:  
 $p(\boldsymbol{y}|\boldsymbol{X}) = \operatorname{softmax}_{\boldsymbol{z}\in Y^N} (s(\boldsymbol{X},\boldsymbol{z}))_{\boldsymbol{y}}.$ 

The probability  $\log p(\boldsymbol{y}_{\text{gold}}|\boldsymbol{X})$  can be efficiently computed using dynamic programming in a differentiable way, so it can be used in NLL computation.

For more details, see Lecture 8 of NPFL114 2022/23 slides.

CTC

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#### **Connectionist Temporal Classification**

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Let us again consider generating a sequence of  $y_1, \ldots, y_M$  given input  $x_1, \ldots, x_N$ , but this time  $M \leq N$ , and there is no explicit alignment of x and y in the gold data.



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#### **Connectionist Temporal Classification**

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We enlarge the set of the output labels by a - (blank), and perform a classification for every input element to produce an **extended labeling** (in contrast to the original **regular labeling**). We then post-process it by the following rules (denoted as  $\mathcal{B}$ ):

1. We collapse multiple neighboring occurrences of the same symbol into one. 2. We remove the blank -. baba" mine hit ... - - 555 adada - - - 5ba - - " Because the explicit alignment of inputs and labels is not known, we consider all possible alignments. — 2nse exp. mnsh s alignmentsDenoting the probability of label l at time t as  $p_l^t$ , we define > past, ze v cuse t Choi uggenerount label l  $lpha^t(s) \stackrel{ ext{def}}{=} \quad \sum \quad \prod p^i_{\pi_i}.$ extended i=1labelings  $\pi$ :  $\mathcal{B}(oldsymbol{\pi}_{1:t}) {=} oldsymbol{y}_{1:s}$ legympti chtel , aa", musin tron mit "a-a", tedy tron musi hyt ales pour jeden blank meni

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#### Computation

When aligning an extended labeling to a regular one, we need to consider whether the extended labeling ends by a *blank* or not. We therefore define

and compute  $lpha^t(s)$  as  $lpha^t_-(s)+lpha^t_*(s).$ 

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### **Connectionist Temporal Classification**

# **Computation** – Initialization

We initialize  $\alpha^1$  as follows:

- $\alpha_{-}^{1}(0) \leftarrow p_{-}^{1}$  } m show the m and m
- all other  $\alpha^1$  to zeros

# **Computation – Induction Step**

We then proceed recurrently according to:

 $\bullet \hspace{0.2cm} \alpha_{-}^{t}(s) \leftarrow p_{-}^{t} \left( \alpha_{*}^{t-1}(s) \right) + \alpha_{-}^{t-1}(s) \right)$ •  $\alpha_*^t(s) \leftarrow \begin{cases} \hline p_{y_s}^t(\alpha_*^{t-1}(s) + \alpha_-^{t-1}(s-1)) + \alpha_*^{t-1}(s-1)) \\ p_{y_s}^t(\alpha_*^{t-1}(s) + \alpha_-^{t-1}(s-1) + \alpha_*^{t-1}(s-1)) \end{cases}$ , if  $y_s \neq y_{s-1}$  by  $t \neq y_{s-1}$  by  $t \neq y_{s-1}$ .

We can write the update as  $p_{y_s}^t ig( lpha_*^{t-1}(s) + lpha_-^{t-1}(s-1) + [y_s 
eq y_{s-1}] \cdot lpha_*^{t-1}(s-1) ig).$ 

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 $\propto$  (3)

N.N.C

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1 2 3 T-2 T-1 T toke Figure 7.3 of "Supervised Sequence Labelling with Recurrent Neural Networks" dissertation by Alex Graves

#### **CTC** Decoding

Unlike BIO-tag structured prediction, nobody knows how to perform CTC decoding optimally in polynomial time.

The key observation is that while an optimal extended labeling can be extended into an optimal labeling of a greater length, the same does not apply to a regular labeling. The problem is that regular labeling corresponds to many extended labelings, which are modified each in a different way during an extension of the regular labeling.





#### **CTC** Decoding



#### Beam Search

To perform a beam search, we keep k best **regular** (non-extended) labelings. Specifically, for each regular labeling  $\boldsymbol{y}$  we keep both  $\alpha_{-}^{t}(\boldsymbol{y})$  and  $\alpha_{*}^{t}(\boldsymbol{y})$ , which are probabilities of all (modulo beam search) extended labelings of length t which produce the regular labeling  $\boldsymbol{y}$ ; we therefore keep k regular labelings with the highest  $\alpha_{-}^{t}(\boldsymbol{y}) + \alpha_{*}^{t}(\boldsymbol{y})$ .

To compute the best regular labelings for a longer prefix of extended labelings, for each regular labeling in the beam we consider the following cases:

- adding a *blank* symbol, i.e., contributing to  $lpha_{-}^{t+1}(m{y})$  both from  $lpha_{-}^t(m{y})$  and  $lpha_{*}^t(m{y})$ ;
- adding a non-blank symbol, i.e., contributing to α<sup>t+1</sup><sub>\*</sub>(•) from α<sup>t</sup><sub>-</sub>(y) and contributing to a possibly different α<sup>t+1</sup><sub>\*</sub>(•) from α<sup>t</sup><sub>\*</sub>(y).

Finally, we merge the resulting candidates according to their regular labeling, and keep only the k best. Roybych si nepanatoral k-nejlepsich, de viscolary, tak je to optimalni. Jenze toho je exp. moc.

 $\sum$ 53 X \* d - X \* V X \* er tohle sjeden Kin. A dose si put nechon le nejlepštet Gjederoengoh. Pot zyšujich se "te" se priblizuja ti option.

#### **Unsupervised Word Embeddings**

The embeddings can be trained for each task separately.

However, a method of precomputing word embeddings have been proposed, based on *distributional hypothesis*:

Words that are used in the same contexts tend to have similar meanings.

The distributional hypothesis is usually attributed to Firth (1957):

You shall know a word by a company it keeps.

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#### Word2Vec





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Word2Vec — tohle je husty

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Table 8: Examples of the word pair relationships, using the best word vectors from Table 4 (Skipgram model trained on 783M words with 300 dimensionality).

		E 1.2		
Relationship Example 1		Example 2	Example 3	
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee	
big - bigger	small: larger	cold: colder	quick: quicker	
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii	
Einstein - scientist	Einstein - scientist Messi: midfielder		Picasso: painter	
Sarkozy - France Berlusconi: Ital		Merkel: Germany	Koizumi: Japan	
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium	
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack	
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone	
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs	
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza	

Table 8 of "Efficient Estimation of Word Representations in Vector Space", https://arxiv.org/abs/1301.3781

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Co ta tabulha nahoir dela:

- Lostma example, litenç se vojter velutorem:

v Pans Fmuee Haly 22 ν a stejný velutor, veprezentnýšcí "hlavní město", - resp. veletor toho smēm "hlavní měste" se pourrije na jing staty a hledome nijblizi slow, liter se v tons prestor melliz.

#### Word2Vec – SkipGram Model





Considering input word  $w_i$  and output  $w_o$ , the Skip-gram model defines

$$p(w_o|w_i) \stackrel{ ext{\tiny def}}{=} rac{e^{oldsymbol{V}_{w_i}^ op oldsymbol{W}_{w_o}}}{\sum_w e^{oldsymbol{V}_{w_i}^ op oldsymbol{W}_w}}.$$

After training, the final embeddings are the rows of the *V* matrix. NPFL138, Lecture 9 Span Labeling CTC CTCDecoding Word2Vec CLEs Subword Embeddings

#### Word2Vec – Hierarchical Softmax

Instead of a large softmax, we construct a binary tree over the words, with a sigmoid classifier for each node.

If word w corresponds to a path  $n_1, n_2, \ldots, n_L$ , we define

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# Word2Vec - Negative Sampling - table se ale pourting minic

Instead of a large softmax, we could train individual sigmoids for all words.

We could also only sample several *negative examples*. This gives rise to the following *negative* sampling objective (instead of just summing all the sigmoidal losses):

$$\frac{1}{2} \frac{1}{2} \frac{1}$$

Violo  $\leq wy^{yell}$  jen negative negative samples k is 5, but it can be even 2 for extremely large corpora.

Each expectation in the loss is estimated using a single sample.

For P(w), both uniform and unigram distribution U(w) work, but

Som musim what  $U(w)^{3/4} - uniformi vzdetan$  $Som musim what <math>U(w)^{3/4} - uniformi vzdetan$ outperforms them significantly (this fact has been reported in several papers by different3/4 je empirietny zrolené authors).

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A Muéluntan je tahová éve malá la chačí port, že tuácé clous se i tak čusto zůčastaní j. ko "negrativní" som pe, tadíč chaný gradinat se tané dostateční thačit doké

ale zase ne mec."

Histo 1000 000 portan notion l+ le signoidé

#### **Recurrent Character-level WEs**



Junguije to troching.	increased	John	Noahshire	phding
i pro nermina slom	reduced	Richard	Nottinghamshire	mixing
V Ý	improved	George	Bucharest	modelling
nle num to uplue ono.	expected	James	Saxony	styling
	decreased	Robert	Johannesburg	blaming
	targeted	Edward	Gloucestershire	christening

Table 2: Most-similar in-vocabular words under the C2W model; the two query words on the left are in the training vocabulary, those on the right are nonce (invented) words.

Table 2 of "Finding Function in Form: Compositional Character Models for Open Vocabulary Word Representation", https://arxiv.org/abs/1508.02096

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#### **Convolutional Character-level WEs**



	In Vocabulary				Out-of-Vocabulary			
	while	his	уои	richard	trading	computer-aided	misinformed	looooook
	although	your	conservatives	jonathan	advertised	_	_	_
LSTM-Word	letting	her	we	robert	advertising	_	_	_
	though	my	guys	neil	turnover	_	_	_
	minute	their	i	nancy	turnover	_	—	_
	chile	this	your	hard	heading	computer-guided	informed	look
LSTM-Char	whole	hhs	young	rich	training	computerized	performed	cook
(before highway)	meanwhile	is	four	richer	reading	disk-drive	transformed	looks
	white	has	youth	richter	leading	computer	inform	shook
	meanwhile	hhs	we	eduard	trade	computer-guided	informed	look
LSTM-Char	whole	this	your	gerard	training	computer-driven	performed	looks
(after highway)	though	their	doug	edward	traded	computerized	outperformed	looked
	nevertheless	your	i	carl	trader	computer	transformed	looking

**Table 6:** Nearest neighbor words (based on cosine similarity) of word representations from the large word-level and character-level (before and after highway layers) models trained on the PTB. Last three words are OOV words, and therefore they do not have representations in the word-level model.

Table 6 of "Character-Aware Neural Language Models", https://arxiv.org/abs/1508.06615

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#### **Character N-grams**

Another simple idea appeared simultaneously in three nearly simultaneous publications as <u>Charagram</u>, <u>Subword Information</u> or <u>SubGram</u>.

A word embedding is a sum of the word embedding plus embeddings of its character *n*-grams. Such embedding can be pretrained using same algorithms as word2vec.

The implementation can be

- dictionary based: only some number of frequent character *n*-grams is kept;
- hash-based: character *n*-grams are hashed into K buckets (usually  $K \sim 10^6$  is used).

Word2Vec



#### **Charagram WEs**



S	un Sword	information	ship you				
	query	tiling	tech-rich	english-born	micromanaging	eateries	dendritic
(	sisg	tile tilooring	tech-dominated tech-heavy	british-born polish-born	micromanage micromanaged	restaurants eaterie	dendrite dendrites
	sg	bookcases built-ins	technology-heavy .ixic	most-capped ex-scotland	defang internalise	restaurants delis	epithelial p53

Table 7: Nearest neighbors of rare words using our representations and skipgram. These hand picked examples are for illustration.

Table 7 of "Enriching Word Vectors with Subword Information", https://arxiv.org/abs/1607.04606

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#### **Charagram WEs**





Figure 2: Illustration of the similarity between character *n*-grams in out-of-vocabulary words. For each pair, only one word is OOV, and is shown on the *x* axis. Red indicates positive cosine, while blue negative.
Figure 2 of "Enriching Word Vectors with Subword Information", https://arxiv.org/abs/1607.04606

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#### **FastText**

The word2vec enriched with subword embeddings is implemented in publicly available fastText library <u>https://fasttext.cc/</u>.

Pre-trained embeddings for 157 languages (including Czech) trained on Wikipedia and CommonCrawl are also available at <u>https://fasttext.cc/docs/en/crawl-vectors.html</u>.

Tohle je hodně dobí 🔽

CTCDecoding



#### **ELMo**

At the end of 2017, a new type of *deep contextualized* word representations was proposed by Peters et al., called ELMo, **E**mbeddings from Language **Mo**dels.

The ELMo embeddings were based on a two-layer pre-trained LSTM language model, where a language model predicts following word based on a sentence prefix. Specifically, two such models were used, one for the forward direction and the other one for the backward direction.



# To compute an embedding of a word in a sentence, the concatenation of the two language model's hidden states is used.



http://jalammar.github.io/images/elmo-embedding.png

ELMo

To be exact, the authors propose to take a (trainable) weighted combination of the input embeddings and outputs on the first and second LSTM layers.

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#### **ELMo Results**



Pre-trained ELMo embeddings substantially improved several NLP tasks.

TASK	<b>PREVIOUS SOTA</b>		OUR BASELINH	ELMO + E baseline	INCREASE (ABSOLUTE/ RELATIVE)
SQuAD	Liu et al. (2017)	84.4	81.1	85.8	4.7 / 24.9%
SNLI	Chen et al. (2017)	88.6	88.0	$88.7\pm0.17$	0.7 / 5.8%
SRL	He et al. (2017)	81.7	81.4	84.6	3.2 / 17.2%
Coref	Lee et al. (2017)	67.2	67.2	70.4	3.2/9.8%
NER	Peters et al. (2017)	$91.93\pm0.19$	90.15	$92.22\pm0.10$	2.06 / 21%
SST-5	McCann et al. (2017)	53.7	51.4	$54.7\pm0.5$	3.3 / 6.8%

Table 1: Test set comparison of ELMo enhanced neural models with state-of-the-art single model baselines across six benchmark NLP tasks. The performance metric varies across tasks – accuracy for SNLI and SST-5;  $F_1$  for SQuAD, SRL and NER; average  $F_1$  for Coref. Due to the small test sizes for NER and SST-5, we report the mean and standard deviation across five runs with different random seeds. The "increase" column lists both the absolute and relative improvements over our baseline.

Table 1 of "Deep contextualized word representations", https://arxiv.org/abs/1802.05365