

$$f(x_1, x_2) = 2 - |x_1 - x_2|$$

$$f(0, 0) =_2 10$$

$$f(0, 1) =_2 01$$

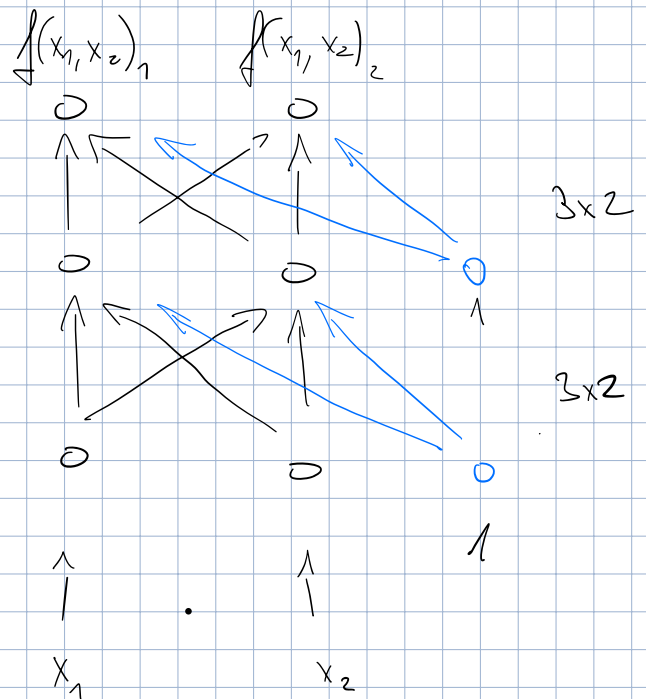
$$f(1, 0) =_2 01$$

$$f(1, 1) =_2 10$$

$$f(x_1, x_2)_1 = \text{NOT XOR}(x_1, x_2)$$

$$f(x_1, x_2)_2 = \text{XOR}(x_1, x_2)$$

$$X \cdot \begin{pmatrix} 1 & -1 \\ -1 & 1 \end{pmatrix} = \vec{0} \quad \sim \text{To mi vyprávě s veličinám 01 říká.}$$



XOR Solution one-bit:

OR(x_1, x_2)

AND

Flipped OR(x_1, x_2)

0	0	0
0	1	1
1	0	1
1	1	1

0	0	1
0	1	1
1	0	1
1	1	0

0	1	0
1	1	1
1	1	1
1	0	0

↖
stačí jeden prvek
pro excitaci

Task 1: Input values $x_i \in \mathcal{N}(\mu, \sigma^2) : \mu=0, \sigma>0$.

Weights initialized from $\langle -a, a \rangle$. What should "a" be?

Is $\mu=0$?

$$\xi = \sum_i^N w_i x_i \quad \mathbb{E}[\xi] = \mathbb{E}\left[\sum_i^N w_i x_i\right] = \sum_i^N \mathbb{E}[w_i] \cdot \mathbb{E}[x_i]$$

Because $x_i \sim \mathcal{N}(0, \sigma^2) \Rightarrow \mathbb{E}[x_i] = 0$,

$w_i \sim \mathcal{U}(-a, a) \Rightarrow \mathbb{E}[w_i] = 0$

then $\mathbb{E}[\xi] = 0$

What should the a be? independent...

$$\begin{aligned} \text{Var}(\xi) &= \text{Var}\left(\sum_i^N w_i x_i\right) = \sum_i^N \text{Var}(w_i x_i) = \sum_i^N \text{Var}(w_i) \cdot \text{Var}(x_i) = \\ &= \sigma^2 \cdot \sum_i^N \text{Var}(w_i) = \sigma^2 \cdot \sum_i^N \frac{4a^2}{12} = \sigma^2 \cdot \sum_i^N \frac{a^2}{3} = N\sigma^2 \cdot \frac{a^2}{3} \end{aligned}$$

$$\text{Var}(\mathcal{U}(a,b)) = \frac{(b-a)^2}{12}$$

If we set $A=1$:

$$1 = N \cdot \sigma^2 \cdot \frac{a^2}{3} \Rightarrow a^2 = \frac{3}{N\sigma^2}$$

$$a = \sqrt{\frac{3}{N\sigma^2}}$$

Therefore the initial weights should be drawn from uniform distr. $\mathcal{U}(-a, a)$, where a is equal

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